NPRG054 High performance software development - 2015/2016 David Bednárek

```
for (i=0; i < N; ++i)
                                 for (i=0; i + 3 < N; i += 4)
                                                                        for (i=0; i + 3 < N; i += 4)
                                                                        {
ł
 a[i] = b[i] + c[i];
                                   a[i] = b[i] + c[i];
                                                                          mm storeu ps(a+i,
}
                                   a[i+1] = b[i+1] + c[i+1];
                                                                            _mm_add_ps(
                                   a[i+2] = b[i+2] + c[i+2];
                                                                              mm loadu ps(b+i),
                                   a[i+3] = b[i+3] + c[i+3];
                                                                              mm loadu ps(c+i));
                                                                        }
                                                                        for (; i < N; ++i)
                                 for (; i < N; ++i)
                                   a[i] = b[i] + c[i];
                                                                          a[i] = b[i] + c[i];
                                 }
                                                                        }
```

- Compilers can vectorize loops
 - Unroll the loop by K iterations
 - Perform the unrolled K iterations in parallel by vector instructions
- but only if some conditions are met

```
for (i=0; i < N; ++i)</pre>
                                 for (i=0; i + 3 < N; i += 4)
                                                                         for (i=0; i + 3 < N; i += 4)
                                                                          ł
  a[i] = b[i] + c[i];
                                   a[i] = b[i] + c[i];
                                                                            _mm_storeu_ps(a+i,
}
                                   a[i+1] = b[i+1] + c[i+1];
                                                                              _mm_add_ps(
                                   a[i+2] = b[i+2] + c[i+2];
                                                                                mm loadu ps(b+i),
                                   a[i+3] = b[i+3] + c[i+3];
                                                                                mm loadu ps(c+i));
                                                                          }
                                                                         for (; i < N; ++i)
                                 for (; i < N; ++i)
                                   a[i] = b[i] + c[i];
                                                                            a[i] = b[i] + c[i];
                                  }
```

- The loop control variable and the condition must be *predictable*
 - Instead of checking the condition for every i, a modified condition is tested for every K-th i
- Compilers often require *countable* loops
 - > The number of iterations must be known (at runtime) before entering the loop
 - Compilers have a built-in list of *countable* loop patterns
 - The source code must match one of these patterns

There shall be no loop-carried dependence

- An iteration must not depend on the result of previous iterations, e.g.:
 - Via a variable
 - Via array positions overlapped by index arithmetics
 - Via overlapping arrays (aliasing)

- Compilers can solve possible loop-carried dependences
 - Test overlapping arrays before entering the loop
 - Additional small overhead

```
i=0;
if ( (a<=b || a>b+3)
  && (a<=c || a>c+3) )
{
    for (; i + 3 < N; i += 4)
    {
        __mm_storeu_ps(a+i,
        __mm_loadu_ps(a+i),
        __mm_loadu_ps(b+i),
        __mm_loadu_ps(c+i)));
    }
}
for (; i < N; ++i)
{
    a[i] = b[i] + c[i];
}
```

- What a loop may do to be useful...
 - Find something and break early
 - Unpredictable condition
 - Accumulate some value in a variable
 - Loop-carried dependence via a variable
 - Generate an output array
 - It might overlap an input array potential loop-carried dependence
- In C/C++, almost no loop can be vectorized as is
 - In Fortran, there is no pointer arithmetics less danger of aliasing
 - The vectorized code can not be strictly equivalent to the original
 - Order of operations must be changed
 - The programmer must help the compiler somehow
 - Often using a pragma that overrides the conservative approach of the compiler
 - The programmer is now responsible for correctness of the vectorization
 - The programmer ensures the absence of aliasing

```
for (i=0; i < N; ++i)
{
    if ( a[i] < b[i] )
        b[i] = b[i] - a[i];
    else
        a[i] = a[i] - b[i];
}</pre>
```

```
for (i=0; i < N; ++i)
{
    c = a[i] < b[i];
    x = b[i] - a[i];
    y = a[i] - b[i];
    b[i] = c ? x : b[i];
    a[i] = c ? a[i] : y;
}</pre>
```

Note:

- This code is not strictly equivalent in parallel environment
- But the same is true for any vectorization due to reordering of memory accesses
- Non-sequentially-equivalent memory models defined in modern parallel programming languages allow to ignore the problem

Vector instructions do not support branching

- No nested loops allowed
- If-then-else allowed only if it can be replaced by masking
 - Both branches are executed for every iteration
 - The result of one branch is masked, i.e. forgotten
 - Like a conditional expression without short-circuit evaluation
 - If one of the branches is significantly larger, the code may execute too many unused computations

Non-contiguous memory access is slow or impossible

• AVX2 supports gather

a[i] = b[c[i]]

• AVX-512 supports scatter

a[b[i]] = c[i]

- Scatter/gather is significantly slower than continuous load/store
 - However faster than scalar memory access
- Scatter is guaranteed to perform writes in the order of increasing lane index i
 - Applies to overlapping write positions. Non-overlapping positions may be written in any order.
- Compiler support is only experimental

• Example: Histogram creation

The vectorized code is not equivalent

- If an index j is present more than once in the vector bb, the result value is incremented only once
 - The fact that scatter operates in a guaranteed order does not help
- Loop-carried dependence in the original code, between writes and subsequent reads from the same a[j]
 - The compiler shall never ignore this dependence
- Remedy: Explicitly check for the repeated indexes using the AVX512CD extension

```
auto ones = mm512 set1 epi32(1);
for (i=0; i + 15 < N; i += 16)
{
  auto bb = _mm512_loadu_epi32(b+i);
  // compute conflicts
  auto cc = mm512 conflict epi32(bb);
  auto cm = _mm512_test_epi32_mask(cc, cc);
  auto m = knot mask16(cm);
  for (;;) {
    // do original action masked by m (where necessary)
    auto aa = mm512 mask i32gather epi32( m, a, bb, 4);
    auto aa1 = _mm512_add_epi32( aa, ones);
    mm512 mask i32scatter ps( m, a, bb, aa1, 4);
    // stop if there were no conflicts
    auto z = kortestz mask16 u8(cm,cm);
    if (z) break;
    // clear lowermost ones in cc (cc = cc & (cc-1))
    auto cc1 = mm512 sub epi32(cc, ones);
    cc = _mm512_and_epi32(cc, cc1);
    // setup new masks
    auto cm1 = mm512 test epi32 mask(cc, cc);
    m = kxor mask16(cm1, cm);
    cm = cm1;
 };
}
for (; i < N; ++i) { ++a[ b[ i]]; }</pre>
```

- *conflict* instruction (AVX512)
 - compares all pairs of lanes for equality
 - triangular matrix returned as i bits in lane i
 - bit j in lane i set if j < i && a[i]==a[j]
- conflict handling
 - detect conflicts (cc)
 - do the required action for lanes having no conflict bit set (m)
 - clear the lowermost conflict bits (these are at the positions just processed)
 - repeat if some conflict bits remain (cm)

- Compiler does not know the alignment of pointers
 - It must emit slow unaligned loads/stores
 - It may generate tests to check whether all pointers are aligned
 - Overhead introduced into the code

• The situation improved since AVX

- Non-aligned load/stores do not cause faults, only longer latency
- The compilers may produce optimistic code without test for alignment
- Applies also for SSE instructions when encoded in VEX encoding (available on AVX-aware CPUs)
 - "-mavx" makes SSE faster!

```
ar = (uintptr t)a \% 16;
br = (uintptr t)b \% 16;
cr = (uintptr t)c \% 16;
if ( ar == br && ar == cr )
{
  for (; i < (16 - ar) % 16 / 4; ++i)
    a[i] = b[i] + c[i];
  for (; i + 3 < N; i += 4)
  {
    _mm_store_ps(a+i,
      _mm_add_ps(
        mm load ps(b+i),
        mm load ps(c+i));
  }
}
else
  for (i=0; i + 3 < N; i += 4)
  {
    mm storeu ps(a+i,
      _mm_add_ps(
        mm loadu ps(b+i),
        mm loadu ps(c+i));
  }
for (; i < N; ++i)
{
  a[i] = b[i] + c[i];
}
```

C/C++ vectorization pragmas

Placed before the loop to be vectorized

#pragma simd

#pragma vector always

#pragma clang loop vectorize(enable)

- Override compiler's decision that vectorizing is possible but not advantageous
 - Often issues warning/error if vectorization failed

#pragma novector

Disable vectorization

#pragma loop count(1000)

Override compiler's estimation of number of iterations

- C/C++ vectorization pragmas
 - Placed before the loop to be vectorized

#pragma ivdep

#pragma GCC ivdep

- Tell the compiler that there are no unprovable loop-carried dependences (via aliasing)
 - Compiler still checks for provable loop-carried dependences (via scalars or index arithmetics)

restrict

 [C99] Declare that a pointer argument is not aliased to any other pointer with the keyword

#pragma vector aligned

Tell the compiler that pointers are always aligned

_declspec(align(16))

__attribute__((aligned(16)))

Enforce alignment of variables, assert alignment of pointers

C/C++ vectorization pragmas

Reduction operators

```
#pragma simd reduction(+:s)
for (i=0; i < N; ++i)
{
   s = s + a[i];
}</pre>
```