



# Modern Database Systems

Advanced Aspects of Big Data Management

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# CAP Theorem

# CAP Theorem

## Recapitulation

### ■ Consistency

- Consistent reads and writes
- Concurrent operations see the same valid and consistent data state

### ■ Availability

- The system is available to serve at the time when it is needed
- Node failures do not prevent survivors from continuing to operate

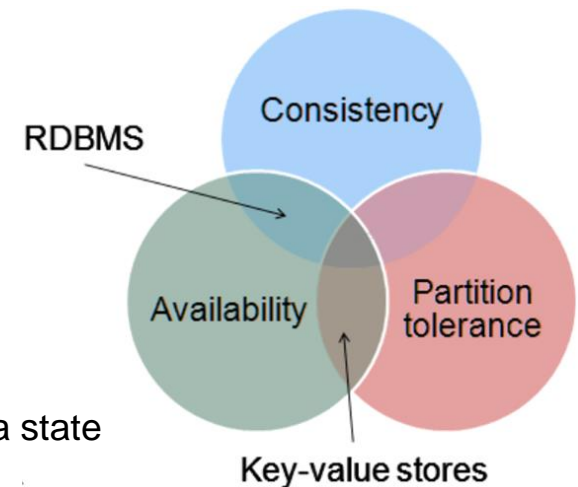
### ■ Partition tolerance

- The ability of a system to continue to service in the event a few of its cluster members become unavailable

### ■ Theorem: In systems that are distributed or scaled out it is impossible to achieve all three.

- First appeared in 1998, published in 1999
- Established as theorem and proved in:

Lynch, Nancy and Gilbert, Seth. *Brewer's conjecture and the feasibility of consistent, available, partition-tolerant web services*. ACM SIGACT News, volume 33 issue 2, 2002, pages 51-59.



# CAP Theorem

## Recapitulation

- **Consistency + Availability**

- Single-site databases, cluster databases, ...

- **Consistency + Partition Tolerance**

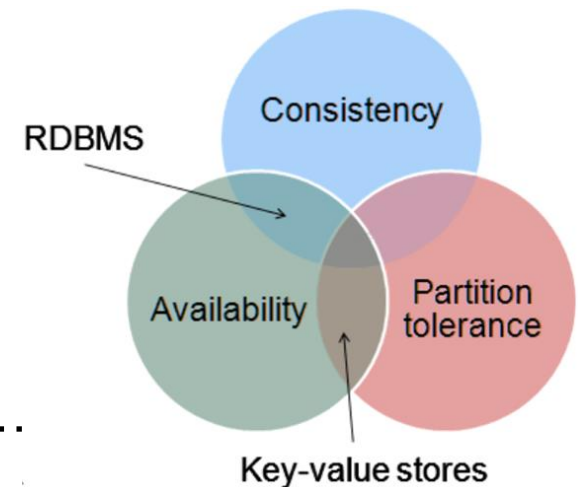
- Distributed databases, distributed locking, majority protocols, ...

- **Availability + Partition Tolerance**

- Web caching, DNS

- **Examples:**

- RDBMS: CA
- Apache Cassandra (column): AP
- Google BigTable (column): CA
- Apache CouchDB (document): AP



# CAP Theorem

## Proof

- Formalization of the notion of consistency, availability and partition tolerance:
  - Atomic **Consistency**, Atomic Data Object
    - There must exist a total order on all operations such that each operation looks as if it were completed at a single instant
      - i.e., any read operation that begins after a write operation completes must return that value
      - Equivalent to requiring requests of the distributed shared memory to act as if they were executing on a single node, responding to operations one at a time
  - **Available** Data Object
    - Every request received by a non-failing node in the system must result in a response
      - i.e., any algorithm must eventually terminate
      - Although we do not say how long it will take
  - **Partition Tolerance**
    - The network is allowed to lose arbitrarily many messages sent from one node to another

# CAP Theorem

## Proof

No clock, nodes make decisions on the basis of **messages** and **local computations**

**Theorem 1.** It is impossible in the asynchronous network model to implement a read/write data object that guarantees the following properties:

- Availability
- Atomic consistency

in all fair executions (including those in which messages are lost).

**Proof (by contradiction).** Assume an algorithm  $A$  exists that meets the three criteria: atomicity, availability, and partition tolerance. We construct an execution of  $A$  in which there exists a request that returns an inconsistent response.

- Assume that the network consists of at least two nodes  $\Rightarrow$  it can be divided into two disjoint, non-empty sets  $G_1$  and  $G_2$ .
- Assume that all messages between  $G_1$  and  $G_2$  are lost.
- If a write occurs in  $G_1$ , and later a read occurs in  $G_2$ , then the read operation cannot return the results of the earlier write operation.

More formally...

# CAP Theorem

## Proof

- Let  $v_0$  be the initial value of the atomic object.
- Let  $\alpha_1$  be the prefix of an execution of  $A$  in which a single write of a value not equal to  $v_0$  occurs in  $G_1$ , ending with the termination of the write operation.
- Assume that no other client requests occur in either  $G_1$  or  $G_2$ , no messages from  $G_1$  are received in  $G_2$  and vice versa.
- We know that this write completes, by the availability requirement.
- Let  $\alpha_2$  be the prefix of an execution in which a single read occurs in  $G_2$ , and no other client requests occur, ending with the termination of the read operation.
- During  $\alpha_2$  no messages from  $G_2$  are received in  $G_1$  and vice versa.
- Again we know that the read returns a value by the availability requirement. The value returned by this execution must be  $v_0$ , as no write operation has occurred in  $\alpha_2$ .
- Let  $\alpha$  be an execution beginning with  $\alpha_1$  and continuing with  $\alpha_2$ .
- To the nodes in  $G_2$ ,  $\alpha$  is indistinguishable from  $\alpha_2$ , as all the messages from  $G_1$  to  $G_2$  are lost, and  $\alpha_1$  does not include any client requests to nodes in  $G_2$ . Therefore in the  $\alpha$  execution, the read request (from  $\alpha_2$ ) must still return  $v_0$ .
- However the read request does not begin until after the write request (from  $\alpha_1$ ) has completed. This therefore contradicts the atomicity property, proving that no such algorithm exists.



# CAP Theorem

## Proof

**Corollary.** It is impossible in the asynchronous network model to implement a read/write data object that guarantees the following properties:

- Availability, in all fair executions,
- Atomic consistency, in fair executions in which no messages are lost.

**Proof.** Main idea: In the asynchronous model an algorithm has no way of determining whether a message has been lost, or has been arbitrarily delayed (atomic consistency when no messages are lost => atomic consistency in all executions => violation of Theorem 1).

- For the sake of contradiction assume that there exists an algorithm  $A$  that always terminates, and guarantees atomic consistency in fair executions in which all messages are delivered.
- Theorem 1 implies that  $A$  does not guarantee atomic consistency in all fair executions, so there exists some fair execution of  $A$  in which some response is not consistent. I.e., at some finite point  $\alpha$  in execution the algorithm  $A$  returns a response that is not atomic consistent.
- Let  $\alpha'$  be the prefix of ending with the invalid response. Next, extend  $\alpha'$  to a fair execution  $\alpha''$ , in which all messages are delivered. The execution  $\alpha''$  is now a fair execution in which all messages are delivered. However this execution is not atomic. Therefore no such algorithm  $A$  exists.





# CAP Theorem

## Proof

- In the real world, most networks are not purely asynchronous
  - Partially Synchronous Networks
    - Each node in the network has a clock
    - All clocks increase at the same rate
    - The clocks are not synchronized
- ⇒ Clocks = timers = can measure how much time has passed
- Can be used for scheduling
  - Every message is either delivered within a given, known time  $t_{msg}$  or it is lost

# CAP Theorem

## Proof

**Theorem 2.** It is impossible in the partially synchronous network model to implement a read/write data object that guarantees the following properties:

- Availability
- Atomic consistency

in all executions (even those in which messages are lost).

**Proof (similar to Theorem 1).** We divide the network into two components  $G_1$  and  $G_2$  and construct an admissible execution in which a write happens in one component, followed by a read operation in the other component. This read operation can be shown to return inconsistent data.

- More formally...

# CAP Theorem

## Proof

- We will construct execution  $\alpha_1$  as in Theorem 1: a single write request and acknowledgment in  $G_1$ , whereas all messages between  $G_1$  and  $G_2$  are lost.
- We will construct the second execution  $\alpha'_2$  slightly differently: Let  $\alpha'_2$  be an execution that begins with a long interval of time during which no client requests occur. This interval must be at least as long as the entire duration of  $\alpha_1$ .
- Then append to  $\alpha'_2$  the events of  $\alpha_2$ , as defined in Theorem 1: a single read request and response in  $G_2$ , again assuming all messages between the two components are lost.
- Finally, construct by superimposing the two executions  $\alpha_1$  and  $\alpha'_2$ .
- The long interval of time in  $\alpha_2$  ensures that the write request in  $\alpha_1$  completes before the read request in  $\alpha'_2$  begins.
- However, as in Theorem 1, the read request returns the initial value, rather than the new value written by the write request, violating atomic consistency.



# CAP Theorem

## Proof

- Analogue of corollary does not hold in partially synchronous model
  - The proof depends on nodes being unaware of when a message is lost



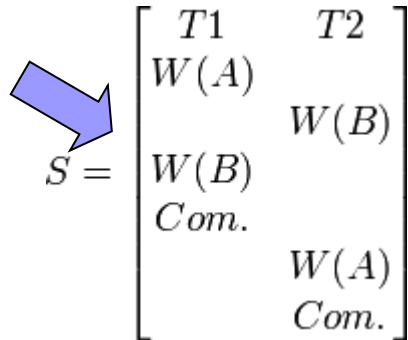
# Managing Transactions

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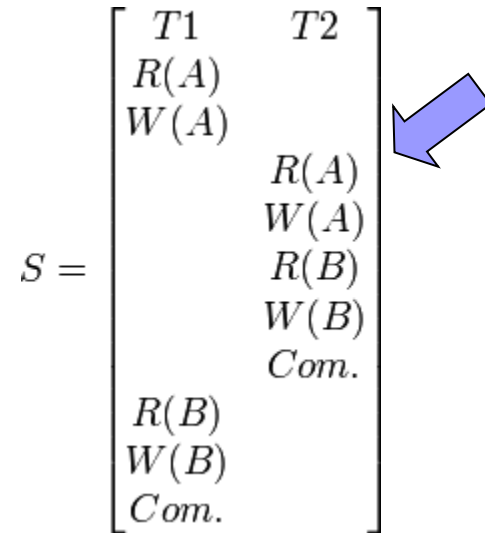
- Critics of NoSQL databases focus on the lack of support for transactions
- Business transaction
  - e.g., browsing a product catalogue, choosing a bottle of Talisker at a good price, filling in credit card information, and confirming the order
- System transaction
  - At the end of the interaction with the user
  - Locks are only held for a short period of time
- Business transaction = a series of system transactions

# Managing Transactions

- **Offline concurrency** involves manipulating data for a business transaction that spans multiple data requests
  - Having a system transaction open for the whole business transaction is not usually possible
    - Long system transactions are not supported
- **Problems:**
  - **Overwriting uncommitted data**
    - More transactions select the same row and then update the row based on the value originally selected unaware of the other
  - **Reading uncommitted data**
    - A transaction accesses the same row several times and reads different data each time
- i.e., calculations and decisions may be made based on data that is changed
  - e.g., price list may be updated, someone may update the customer's address, changing the shipping charges, ...



overwriting uncommitted data  
(blind write)



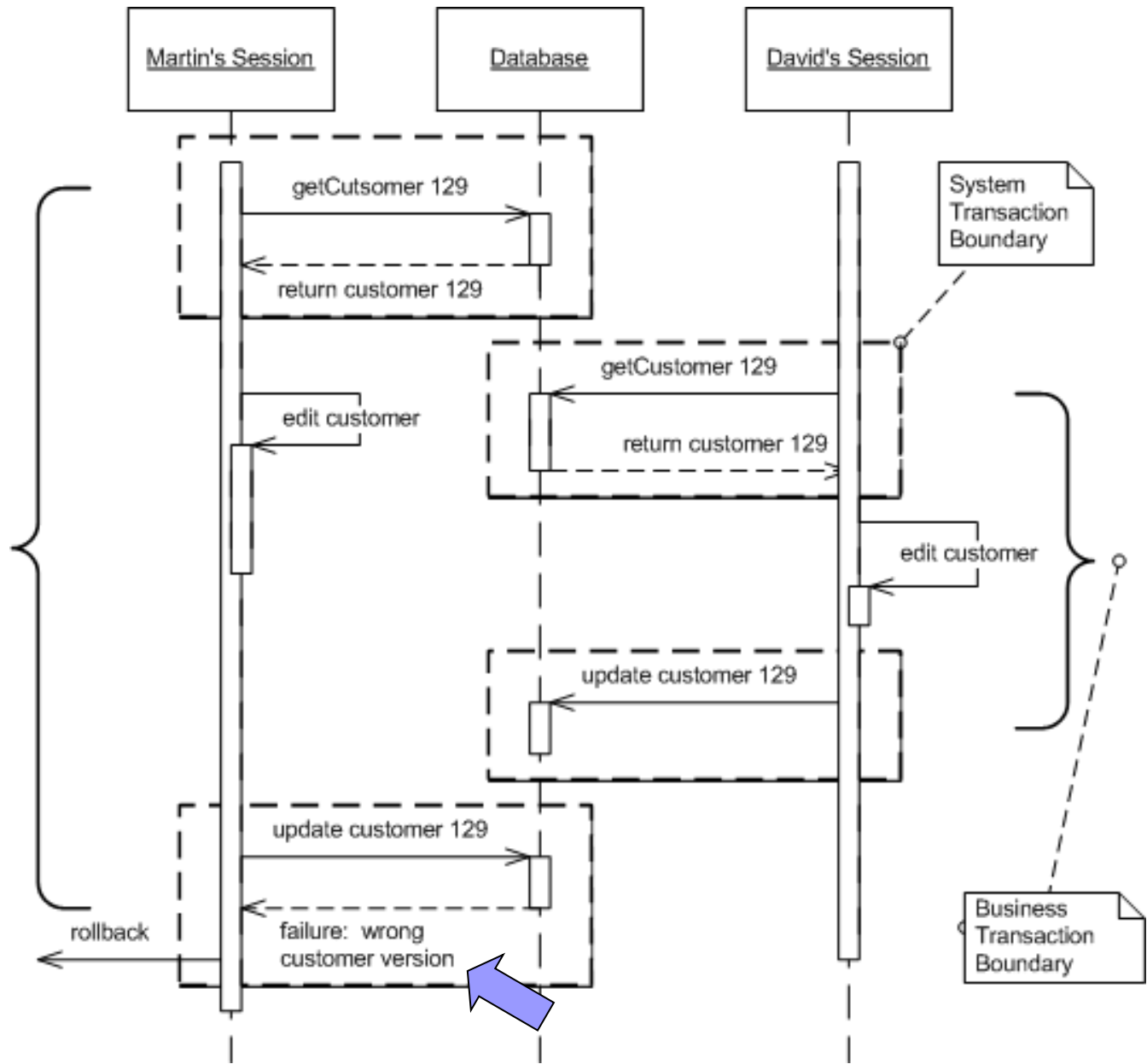
reading uncommitted data  
(dirty read)



# Managing Transactions

## Optimistic Offline Lock

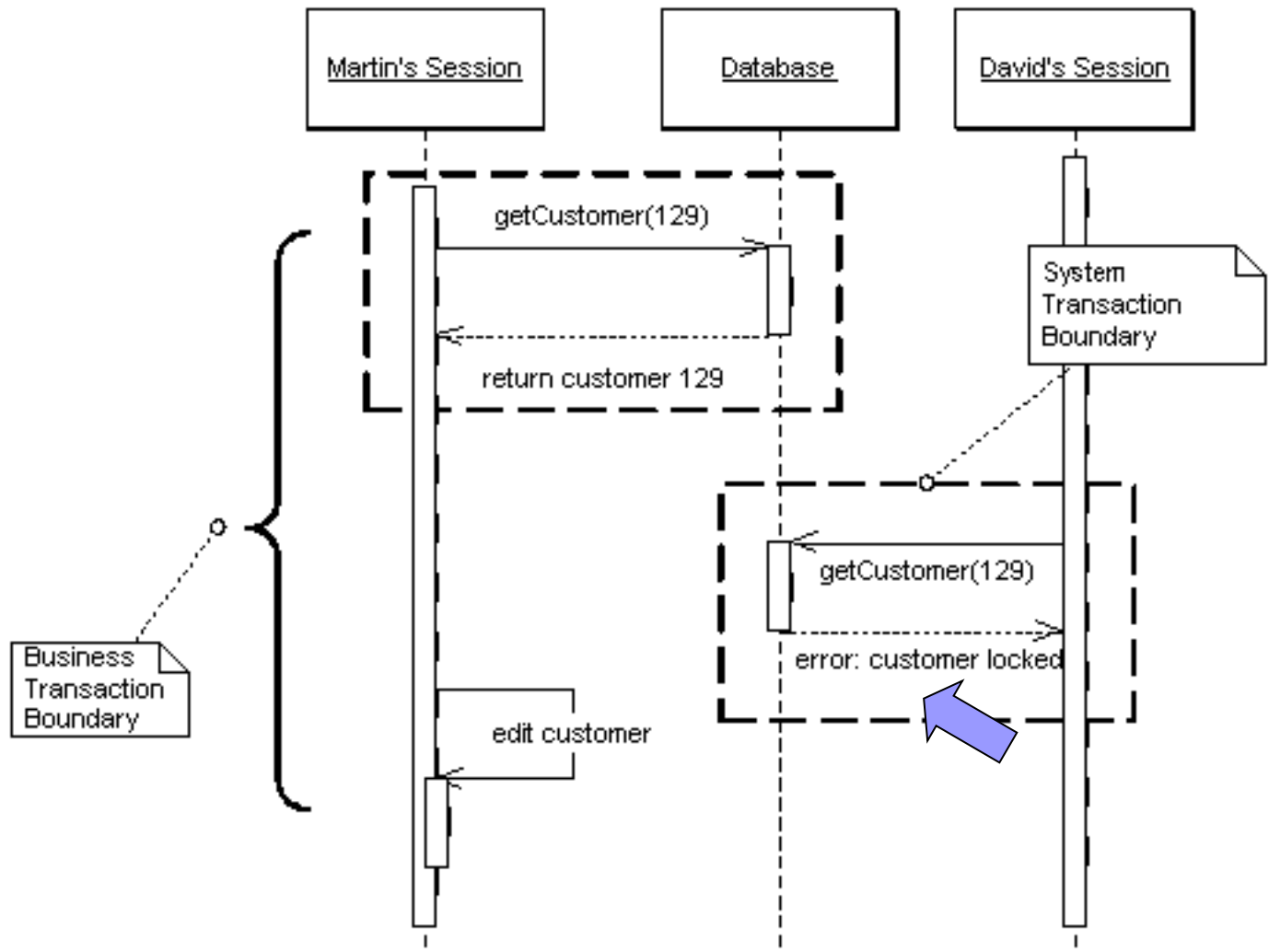
- Assumes that the chance of conflict is low
- A form of conditional update
  - Ensures that changes about to be committed by one session do not conflict with the changes of another session
- Pre-commit validation
  1. Client operation re-reads any information that the business transaction relies on
  2. It checks that it has not changed since it was originally read and displayed to the user
- Obtaining a lock indicating that it is okay to go ahead with the changes to the record data



# Managing Transactions

## Pessimistic Offline Lock

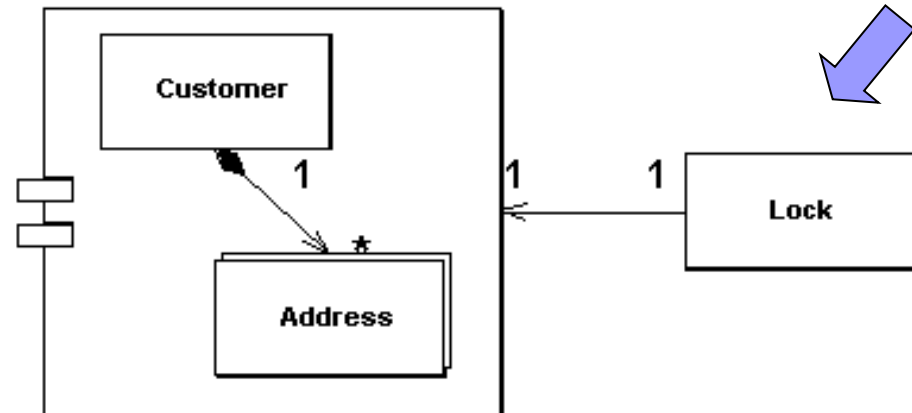
- Problems of optimistic approach:
  - There might be many conflicts
  - The conflict can be detected at the end of a lengthy business transaction
- Pessimistic solution: allows only one business transaction at a time to access data
- Forces a business transaction to acquire a lock on each piece of data before it starts to use it
  - Once a business transaction begins, it surely completes
- Lock manager
  - Simple, single (for all business transactions), centralized (or based on the database in the distributed system)
- Standard issue: **deadlock**
  - Timeout for an application
    - Automatically rolled-back after a period of time of non responding
  - Timestamp attribute for a lock
    - Automatically released after a period of time



# Managing Transactions

## Coarse-grained Lock

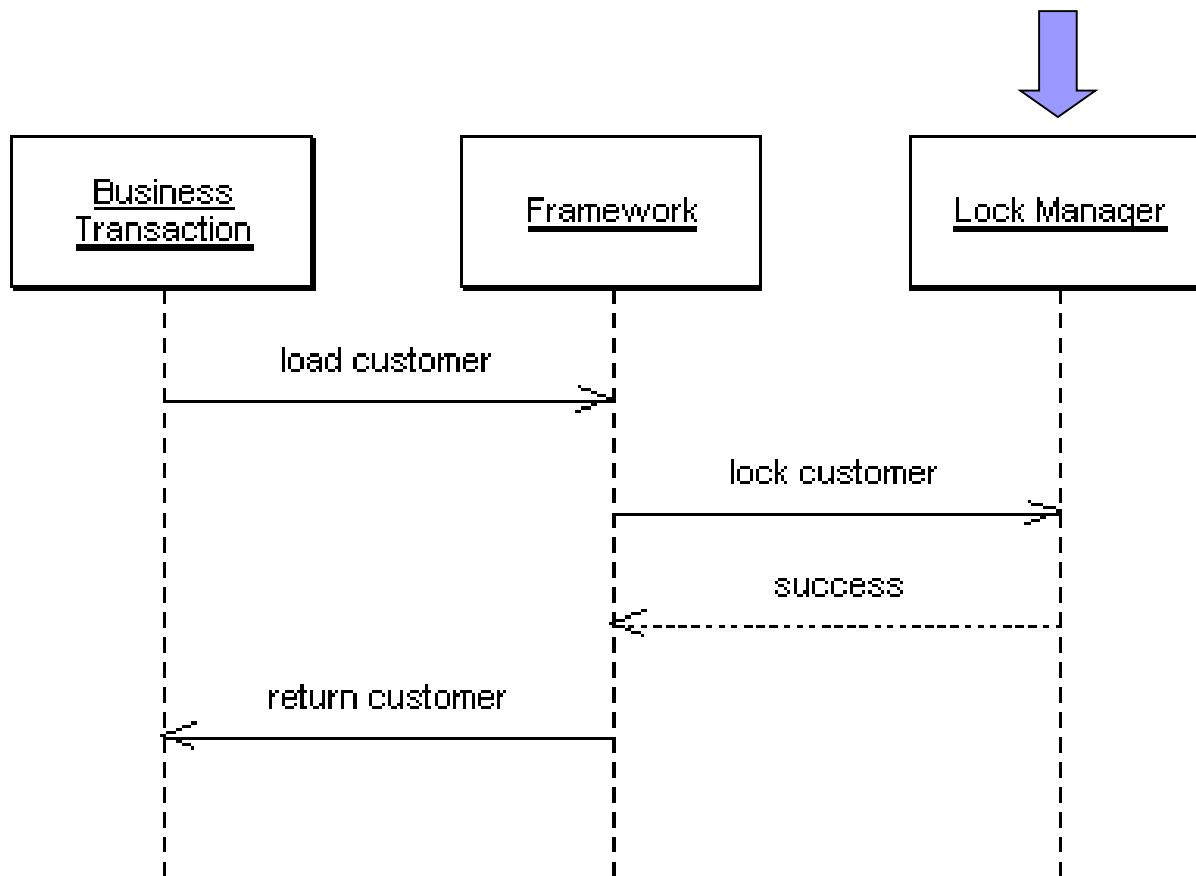
- When objects are edited as a group
  - Logically related objects
  - e.g., a customer and its set of addresses
    - We want to lock any one of them
- A separate lock for individual objects presents a number of challenges
  - We need to find them all in order to lock them
    - Gets tricky as we get more locking groups
    - When the groups get complicated
      - Nested groups
- Idea: a single lock that covers many objects
  - A sophisticated lock manager




# Managing Transactions

## Implicit Lock

- Problem: forgetting to write a single line of code that acquires a lock  $\Rightarrow$  entire offline locking scheme is useless
  - Failing to retrieve a read lock  $\Rightarrow$  other transactions use write locks  $\Rightarrow$  not getting up-to-date session data
  - Failing to use a version count  $\Rightarrow$  unknowingly writing over someone's changes
  - Not releasing locks  $\Rightarrow$  bring productivity to a halt
- Fact: If an item might be locked anywhere it must be locked everywhere
- Idea: locks are automatically acquired
  - Not explicitly by developers but implicitly by the application





# Performance Tuning



# Performance Tuning Goals

**Example from 2010:** Tweets add up to 12 Terabytes per day. This amount of data needs around 48 hours to be written to a disk at a speed of about 80 Mbps.

- MapReduce creates a bottleneck-free way of scaling out
- To reduce latency
  - Latency:
    - Non-parallel systems: time taken to execute the entire program
    - Parallel systems: time taken to execute the smallest atomic sub-task
  - Strategies:
    - Reducing the execution time of a program
    - Choosing the most optimal algorithms for producing the output
    - Parallelizing the execution of sub-tasks
- To increase throughput
  - Throughput = the amount of input that can be manipulated to generate output within a process
  - Non-parallel systems:
    - Constrained by the available resources (amount of RAM, number of CPUs)
  - Parallel systems:
    - “No” constraints
    - Parallelization allows for any amount of commodity hardware

# Performance Tuning

## Linear Scalability

- Typical horizontally scaled MapReduce-based model:  
linear scalability
  - “One node of a cluster can process  $x$  MBs of data every second  
→  $n$  nodes can process  $x \times n$  amounts of data every second.”
    - Time taken to process  $y$  amounts of data on a single node =  $t$  seconds
    - Time taken to process  $y$  amounts of data on  $n$  nodes =  $t/n$  seconds
- Assumption: tasks can be parallelized into equally balanced units

# Performance Tuning

$$S(N) = \frac{1}{(1 - P) + \frac{P}{N}}$$

## Amdahl's Law

- Formula for finding the maximum improvement in performance of a system when a part is improved
  - $P$  = the proportion of the program that is parallelized
  - $1 - P$  = the proportion of the program that cannot be parallelized
  - $N$  = the times the parallelized part performs as compared to the non-parallelized one
    - i.e., how many times faster it is
      - e.g., the number of processors
    - Tends to infinity in the limit
- Example: a process that runs for 5 hours (300 minutes); all but a small part of the program that takes 25 minutes to run can be parallelized
  - Percentage of the overall program that can be parallelized: 91.6%
  - Percentage that cannot be parallelized: 8.4%
  - Maximum increase in speed:  $1 / (1 - 0.916) = \sim 11.9$  times faster
    - $N$  tends to infinity

# Performance Tuning

$$L = kW$$

## Little's Law

- Origins in economics and queuing theory (mathematics)
- Analyzing the load on stable systems
  - Customer joins the queue and is served (in a finite time)
- “The average number of customers ( $L$ ) in a stable system is the product of the average arrival rate ( $k$ ) and the time each customer spends in the system ( $W$ ).”
  - Intuitive but remarkable result
  - i.e., the relationship is not influenced by the arrival process distribution, the service distribution, the service order, or practically anything else
- Example: a gas station with cash-only payments over a single counter
  - 4 customers arrive every hour
  - Each customer spends about 15 minutes (0.25 hours) at the gas station
  - ⇒ There should be on average 1 customer at any point in time
  - ⇒ If more than 4 customers arrive at the same station, it would lead to a bottleneck

# Performance Tuning

## Message Cost Model

initialization

$$C = a + bN$$

linear dependence  
on size

- Breaks down the cost of sending a message from one end to the other in terms of its fixed and variable costs
  - $C$  = cost of sending the message from one end to the other
  - $a$  = the upfront cost for sending the message
  - $b$  = the cost per byte of the message
  - $N$  = number of bytes of the message
- Example: gigabit Ethernet
  - $a$  is about 300 microseconds = 0.3 milliseconds
  - $b$  is 1 second per 125 MB
    - Implies a transmission rate of 125 MBps.
  - 100 messages of 10 KB => take  $100 \times (0.3 + 10/125)$  ms = 38 ms
  - 10 messages of 100 KB => take  $10 \times (0.3 + 100/125)$  ms = 11 ms
  - A way to optimize message cost is to send as big packet as possible each time

0,08

0,8

# References

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